Glossary of Mathematical Symbols in Order of Appearance

Chapter 1

exponential average

rate of change (in nominal spending) or rate of inflation or rate of return

k parameter setting the elasticity of an exponential average

Chapter 2

money supply m_n

price level p_n

expected value of p_n p_n^e volume of output γ_n

excess demand/liquidity measured in terms of real d_n money balances

demand for real money balances μ

volume of output when $d_n = 0$ $\overline{\gamma}$

Chapter 3

 PUR^{j} intermediate consumption of goods and services of busi-

ness j

Ţj investment of business *j* (or of commercial bank *k*) W^j wages paid out by business j (or by commercial bank k)

 DIV_a^j dividends paid out by business j (or by commercial

bank k)

 INT_{a}^{J} interests paid out by business *j* (or by commercial bank *k*) A_a^j

securities amortized (or redeemed) by business j (or by

commercial bank *k*)

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SEC_{a}^{j}
         securities bought by business j (or by commercial
         bank k)
dM^j
         change in the money balance held by business j
D^{j}
         total applications of funds of business i (excluding dM^{i})
REV^{j}
         sales of goods and services of business j (or of commercial
         bank k)
DIV_{i}^{j}
         dividends received by business j (or by commercial
         bank k)
INT_{i}^{j}
         interests received by business j (or by commercial
         bank k)
A_i^j
         securities amortized (or redeemed) to business j (or to
         commercial bank k)
SEC_{i}^{j}
         securities sold or issued by business j (or by commercial
         bank k)
dL^{j}
         new bank loans raised by business j from commercial
         banks
dL'^{j}
         new loans raised by business j from the central banks
R^{j}
         total sources of funds of business j (excluding dL^{j} and
         dL^{(j)}
M
         broad money supply
M_{M}
         currency
M_{S}
         deposits with commercial banks
M_{hh}
         money balances held by households
         money balances held by the business sector (including
M_h
         commercial banks)
INC_{hh}
         aggregate income of households
C_{hh}
         aggregate consumption of households
SAV<sub>hh</sub>
         aggregate savings of households
CF_h
         retained operating earnings of the business sector
D
         aggregate nominal spending (cash outlays) of all sectors
R_T
         aggregate cash receipts of all sectors
M_T
         transaction balances
M_P
         precautionary balances
         transactions velocity of M
t
         point on the physical (or calendar) time scale
V_P
         transactions velocity of precautionary balances
         transactions velocity of transaction balances
V_T
f(x)
         demand for money function in Allais's 1953 formulation
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- g(x) supply of money function in Allais's 1953 formulation
- M_D desired money balances
- T response period (elementary average planning period for all agents)
- f_m lower limit of the demand for money function
- f_M upper limit of the demand for money function
- g_m lower limit of the supply of money function
- g_M upper limit of the supply of money function
- D_e aggregate nominal spending in a stationary equilibrium

- r continuous constant periodic rate of decay in an exponential average
- V_0 transaction velocity of money in a stationary state
- φ_t notional function used to introduce the relationship between the physical and the psychological time scale as well as the variability of the velocity of money and that of the rate of memory decay
- T_0 response period in a stationary state
- t' a point on the psychological time scale
- χ continuous rate of memory decay along the physical time scale
- χ_0 continuous rate of memory decay along the psychological time scale (or in a stationary state)
- Z coefficient of psychological expansion
- ϕ_0 scaling parameter (ratio of desired balances to nominal spending when Z=0)
- $\Psi(Z)$ relative desired balances, a logistic function of Z
 - b parameter in the function Ψ , setting its maximum value $\phi_0(Z)$
 - α parameter in the function Ψ , setting the slope of $\phi_0(Z)$ the asymptotic limit of its elasticity with respect to Z
 - z dynamic equilibrium rate ("perceived" rate of change)
 - \overline{x} average rate of growth during a period p
 - p time-scaling factor used to compute Z in discrete time
 - Ψ^* estimated value of Ψ
 - β elasticity of expected inflation with respect to actual price changes in Cagan's 1954 formulation

- E expected inflation in Cagan's 1954 formulation
- C actual change in prices in Cagan's 1954 formulation
- α elasticity of the demand for real balances with respect to expected inflation in Cagan's 1954 formulation
- $\overline{\chi}$ elasticity of memorized nominal growth with respect to actual changes in Allais's 1954 formulation
- *u* memorized nominal growth in Allais's 1954 formulation
- K elasticity of the demand for desired balances with respect to memorized nominal growth in Allais's 1954 formulation
- Z_0 initialization parameter, value of Z for t = 0
- P a price or a price index
- ζ_1 expectations of momentum traders in Smith's formulation
- c_1 elasticity of the expectations of momentum traders with respect to price changes in Smith's formulation
- q_1 weight given to momentum traders in Smith's formulation
- ζ_2 price deviation from fundamental value in Smith's formulation
- q₂ weight given to fundamental investors in Smith's formulation
- $k(\zeta)$ total investor sentiment function in Smith's formulation
 - ρ rate of growth in base money
- $\gamma(Z)$ base-money multiplier, a logistic function of Z
- a' parameter in the function γ , setting its minimum value (1-a')
- b' parameter in the function γ , setting its maximum value (1 + a'b')
- α' parameter in the function γ , setting the slope of the asymptotic limit of its elasticity with respect to Z
- B_0 value of base money for t = 0
- q scaling parameter in the money supply function

- Q volume of transactions
- *E* nonbank credit in Allais's fundamental equation of monetary dynamics
- M_{De} demand for money in dynamic equilibrium
- M_e supply of money in dynamic equilibrium
- x_e rate of growth in nominal spending in dynamic equilibrium

- z_e dynamic equilibrium rate
- Z_{e} coefficient of psychological expansion in dynamic equilibrium
- V_e transaction velocity of money in dynamic equilibrium
- χ_e rate of memory decay in dynamic equilibrium
- V_0^* transaction velocity of money in a stationary state
- Θ period of endogenous fluctuations in nominal spending

- x^* estimated rate of growth in nominal spending
- Z^* estimated coefficient of psychological expansion
- *K* ratio of aggregate nominal spending to national income, ratio of the transaction velocity of money to its income velocity
- *v* income velocity of money

Chapter 7

 θ time elapsing between the assessment and the collection of taxes

Chapter 8

- i psychological rate of interest
- j yield on long-term bonds
- i_l pure long-term interest rate
- l_j liquidity premium on long-term bonds
- λ parameter equal to the ratio of the liquidity premium l_j to the nominal interest j
- W an approximation of aggregate nominal spending
- j^* estimated yield on long-term bonds with respect to χ
- μ ratio of the estimated nominal interest rate j^{**} to z
- j^{**} estimated yield on long-term bonds with respect to z
- P price of a share
- do current dividend
- r discount rate of dividends
- g^* expected long-term growth rate of dividend
- π ex-anti equity risk premium

Chapter 9

- O_{MD} outstanding margin debt
- M₃ broad money supply
- ff federal funds rate

- x_{SP} return of the S&P 500 index
- x_N return of the NASDAQ index
- P rescaled ratio of margin debt to broad money supply $O_{
 m MD}/M_3$

- x_i an outcome in a risky prospect
- p_i the probability of outcome x_i
- P a risky prospect consisting of one or several outcomes
- V the psychological value of a risky prospect
- E the mathematical expectation of a risky prospect
- *B* a neo-Bernoullian index of the psychological value of a risky prospect (ignoring its distribution)
- C an individual's capital
- *u* cardinal utility
- w decision weights in prospect theory
- v the psychological value of an outcome in prospect theory
- π the function transforming probabilities into decision weights in prospect theory
- μ_l the *l*th-order moment of a risky prospect
- Allais's cardinal utility (or absolute satisfaction) function
- U_0 an individual's psychological capital
- X the absolute change (gain or loss) in an individual's psychological capital
- U_0^* the statistical estimate of an individual's psychological capital
- $B_{1/2}$ Bernoulli's index for a constant-probability (1/2), variable-gain prospect
- B_{200} Bernoulli's index for a variable-probability, constant-gain (200) prospect
 - R the psychological value of a risky prospect according to Allais, a function of its moments

Chapter 11

 χ_0^i rate of memory decay of age group i in a stationary state



